

### Objectives

- 1) Review order of operations and importance of parentheses in GC calculations
- 2) Review exponents and scientific notation and recognize when GC has switched to scientific notation
- 3) GC practice
  - GC 1
  - GC 2
  - GC 3
  - GC 4
  - GC 6
  - { GC 5

Order of operations

⇒ written in detail on front of GC 3.

Evaluate

$$\textcircled{1} \quad 18 - 4 \div 2 + 5$$

$$= 18 - \frac{4}{2} + 5$$

divide first

$$= 18 - 2 + 5$$

subtract and add from Left to Right

$$= 16 + 5$$

$$= \boxed{21}$$

$$\textcircled{2} \quad \frac{18 - 4}{2 + 5}$$

numerator first (subtract)

denominator second (add)

$$= \frac{14}{7}$$

divide last

$$= \boxed{2}$$

To put these into your GC

$$\textcircled{1} \quad 18 - 4 / 2 + 5 \quad \rightarrow \text{GC knows order of op!}$$

$$\textcircled{2} \quad (18 - 4) / (2 + 5) \quad \rightarrow \text{GC must be told to do add and subtract before divide.}$$

Scientific Notation

Simplify

$$(3) \quad x + x + x = \boxed{3x}$$

repeated addition  
is multiplication

$\Rightarrow$  combine like terms

$$(4) \quad x \cdot x \cdot x = \boxed{x^3}$$

repeated multiplication  
is exponent

$$(5) \quad 10^3 = 10 \cdot 10 \cdot 10 = \boxed{1000}$$

$$(6) \quad 4 \times 10^3 = 4 \times 1000 = \boxed{4000}$$

order of op:  
exp before  
mult.

$$(7) \quad 10^{-3} = \frac{1}{10^3} = \frac{1}{1000} = \boxed{.001}$$

neg exponent  
is a positive exp  
in denominator

$$(8) \quad 4 \times 10^{-3} = 4 \times .001 = \boxed{.004}$$

# Scientific Notation Summary for Math 70

## Objectives

- 1) Given a number in standard form, write it in scientific notation.
  - a) If small number ( $<1$ ), negative exponent
  - b) If large number ( $\geq 10$ ), positive exponent
- 2) Given a number in scientific notation, write in standard form.  
Method: Multiply.
- 3) Use scientific notation to make calculations easier.
- 4) Write results of calculations in scientific notation.

Scientific Notation: A number written as  $a \times 10^N$ , where

a)  $N$  is an integer  $\{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$

b)  $|a| > 0$  but  $|a| < 10$ .

NONZERO

(This means:  $a$  has one digit to the left of the decimal pt.)

Examples: These numbers are in scientific notation.

①  $2.035 \times 10^4$

means 20350

②  $1.98 \times 10^0$

means 1.98

③  $4. \times 10^{-2}$

means 0.04

Examples: These numbers aren't quite in scientific notation.

④  $0.34 \times 10^5$

(digit to left of decimal point cannot be zero)

⑤  $13.04 \times 10^{-3}$

← (only one digit to left of decimal pt.)  
↙

⑥  $20.3 \times 10^4$

To write in scientific notation:

⑦ 270,300,000,000.

$2.703 \times 10^?$

270,300,000,000.

↑ ← ← ← ← ← ←  
11 places

$2.703 \times 10^{11}$

Starting from the LEFT,  
find one nonzero digit.

Write the "a" part of  $a \times 10^N$ .

Count the number of decimal  
places moved.

This is the exponent.

## Scientific Notation, p. 2

⑧  $0.0000000306$

$3.06 \times 10^?$

$0.0000000306$

→ → → → → ↑

8 places

$3.06 \times 10^{-8}$

← Very small number;  
a negative power of 10  
is needed.

To write a number in standard form:

⑨  $-3.5701 \times 10^8$

↑  
move decimal  
pt 8 places

$-357010000.$

↓ --- → --- → --- ↑

$-357,010,000.$

multiplying by a positive  
power of 10 makes a  
large number.

(decimal pt moves right)

Move decimal point,  
using as many extra  
zeros as needed.

⑩  $1.02 \times 10^{-6}$

↑  
move decimal  
6 places

$.00000102$

↑ ← ← ← ← ← ↓

$.00000102$

multiplying by a negative  
power of 10 makes a  
small number

(decimal pt moves left)

\* CAUTION \* Be sure your final answer has only one decimal point!

To use scientific notation for calculations (Mult & Divide only)

⑪  $(1.2 \times 10^{12})(3 \times 10^{-4})$

$= (1.2)(10^{12})(3)(10^{-4})$

$= (1.2)(3)(10^{12})(10^{-4})$

$= 3.6 \quad 10^{12-4}$

$= 3.6 \times 10^8$

Note that this is simply  
four numbers, all multiplied.

Commutative property lets  
us change the order

# Scientific Notation, p.3

$$\begin{aligned} (12) \quad & \frac{4.8 \times 10^{-5}}{2 \times 10^{-26}} \\ &= \left( \frac{4.8}{2} \right) \cdot \left( \frac{10^{-5}}{10^{-26}} \right) \\ &\quad \downarrow \quad \downarrow \\ &= (2.4)(10^{-5-(-26)}) \\ &= \boxed{2.4 \times 10^{21}} \end{aligned}$$

Note that we can clarify by rewriting using the definition of fraction multiplication backward.

$$\text{If } \frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd},$$

$$\text{then } \frac{a \times c}{b \times d} = \left( \frac{a}{b} \right) \cdot \left( \frac{c}{d} \right).$$

\* CAUTION \* The result may not be in proper scientific notation.

$$\begin{aligned} (13) \quad & (4 \times 10^{-17})(9 \times 10^{-11}) \\ &= (4)(9)(10^{-17})(10^{-11}) \\ &= 36 \times 10^{-28} \\ &= 3.6 \times 10^1 \times 10^{-28} \\ &= \boxed{3.6 \times 10^{-27}} \end{aligned}$$

← 2 digits to the left of the decimal.

← Substitute for 36 what you get when you write 36 in scientific notation.

$$36 = 3.6 \times 10^1$$

Then add exponents.

$$\begin{aligned} (14) \quad & \frac{1.5 \times 10^{-3}}{3 \times 10^{15}} \\ &= \left( \frac{1.5}{3} \right) \cdot \left( \frac{10^{-3}}{10^{15}} \right) \\ &= \frac{1}{2} \cdot 10^{-3-15} \\ &= 0.5 \times 10^{-18} \end{aligned}$$

← Must have one nonzero digit to the left of the decimal pt.

← Substitute for 0.5 what you get when you write 0.5 in scientific notation:

$$0.5 = 5 \times 10^{-1}$$

$$\begin{aligned} &= 5.0 \times 10^{-1} \times 10^{-18} \\ &= \boxed{5.0 \times 10^{-19}} \end{aligned}$$

Then add exponents.

# Solutions to "Do the Math" Exercises 5.6

- ①  $8 \times 10^9$
- ②  $1 \times 10^{-7}$
- ③  $2.83 \times 10^{-5}$
- ④  $4.01 \times 10^8$
- ⑤  $8 \times 10^0$
- ⑥  $1.2 \times 10^2$
- ⑦ 375
- ⑧ 6,000,000
- ⑨ 0.0005
- ⑩ 0.49
- ⑪ 540,000
- ⑫ 0.005123
- ⑬  $2.4 \times 10^{-8}$
- ⑭  $1 \times 10^4$
- ⑮  $5 \times 10^{-2}$
- ⑯  $4 \times 10^5$
- ⑰  $1.1 \times 10^{-7}$
- ⑱  $2 \times 10^{11}$

## **M70 1.8 & 5.2 Intro to the Graphing Calculator, Review Order of Operations & Scientific Notation**

### **Graphing calculator handouts**

All-in-one problem -- this is the goal, and is remarkably similar to the question on the PQ!

GC 1

GC 2

GC 3

GC 4

GC 6

If you finish all of the above in class, then GC5

GC 5: Examples must be done IN ORDER, or the packet does not make sense.

You may choose from several approaches:

- 1) Challenge first: (Recommended only for students who have used a GC a lot.)

Start with the All-in-one problem. If you don't have the correct answer, review handouts, especially

GC 3 regarding the correct use of parentheses and

GC 2 regarding scientific notation.

Once you have the correct answer, do GC 5.

GC 5: Examples must be done IN ORDER, or the packet does not make sense.

- 2) Systematic: (Recommended for students who are new to the GC or have forgotten.)

Start with GC 1: do all

GC 2: do examples 1-14 first, skip the Practice for now

GC 3: do examples 1-12 first, skip the Practice for now

GC 4: do examples 1-9 first, skip the Practice for now

GC 6: do examples 1-3 first, skip the Practice for now

All-in-one problem

Test yourself – if you need more practices, go back to the Practice problems on GC 2-3-4-6

GC 5: Examples must be done IN ORDER, or the packet does not make sense.

- 3) Review first: (For the impatient student. Not generally recommended.)

Skim all examples, GC1-2-3-4-6

Work on All-in-one problem. . If you don't have the correct answer, review handouts, especially

GC 3 regarding the correct use of parentheses and

GC 2 regarding scientific notation.

Once you have the correct answer do GC 5.

GC 5: Examples must be done IN ORDER, or the packet does not make sense.

Complete GC packets and all solutions are available on the class website under GC Exercises.

Keystrokes for the All-in-one problems are on the class website under Lecture Notes.



## Introduction to the GC

### GC All-in-One Problem

#### handouts

GC1. do all

GC2. do examples 1-14 first  
save practice  
until after you do GC 4

GC3. do examples 1-12 first  
save practice until  
after you do GC 4 examples

GC4 do examples 1-9 first

GC 6 do examples 1-3 first

After doing all worked examples, you may  
choose based on what you need:

a) If you knew this already, look at all  
practice problems GC 2, 3, 4 and do  
only those that seem hard.

Check your answers!

Solutions are provided in packets sometimes  
and online always.

b) If this is all new to you, do practice  
problems for all packets and continue at  
home.

c) If you finish GC1-4, go on to optional  
GC 5.

For those who did not bring a GC,  
complete the essay.

**Note:** GC packets here have all pages, including  
solutions to all practice questions.

Paper packets in class are sometimes missing  
pages.

**Math 70 GC All-In-One problem**

This question uses algebra to evaluate, GC to calculate (including extra parentheses, negative numbers, memory locations, locating obscure roots), scientific notation, standard notation, rounding, determining an exact versus an approximate answer, etc.

- 1) Evaluate  $\frac{97y^9 - 4\sqrt[3]{x}}{908020\sqrt{x} - 993y}$  when  $x = 0.92$  and  $y = -1.06$ , and round to the nearest ten-thousandth.
- 2) Check the box which describes your answer.
  - ☐ My answer is exact.
  - ☐ My answer is approximate.

## Math 70 GC All-In-One problem

This question uses algebra to evaluate, GC to calculate (including extra parentheses, negative numbers, memory locations, locating obscure roots), scientific notation, standard notation, rounding, determining an exact versus an approximate answer, etc.

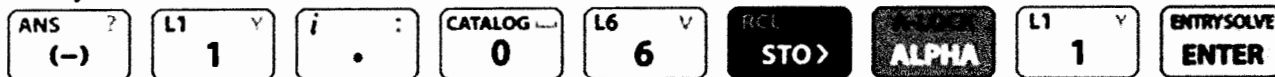
- Evaluate  $\frac{97y^9 - 4\sqrt[3]{x}}{908020\sqrt{x} - 993y}$  when  $x = 0.92$  and  $y = -1.06$ , and round to the nearest ten-thousandth.
- Check the box which describes your answer.  
☐ My answer is exact.  
☒ My answer is approximate.

### SOLUTION

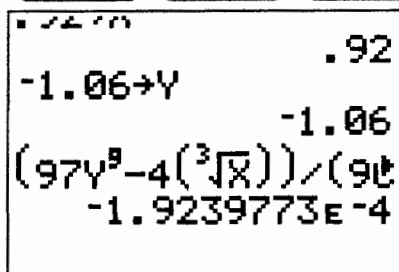
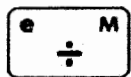
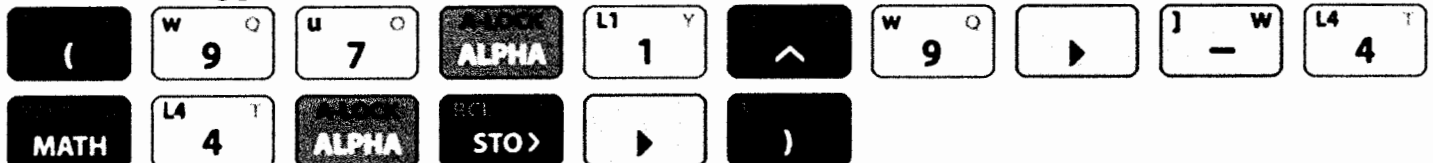
Store x



Store y



Calculation, using parentheses around numerator and parentheses around denominator



Result is in scientific notation!  $-1.9239773E-4$  means  $-1.9239773 \times 10^{-4}$  which means  $-0.00019239773$

This is an approximate answer because

- $0.92$  is not a perfect square so  $\sqrt{0.92}$  is irrational. Its decimal is nonrepeating and nonterminating.
- $0.92$  is not a perfect cube, so  $\sqrt[3]{0.92}$  is irrational. Its decimal is nonrepeating and nonterminating.
- There are almost certainly decimal places beyond the screen which could not be displayed.

Round to the nearest ten-thousandth means four decimal places.






Approximate answer:  $-0.0002$

Name \_\_\_\_\_

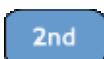

Date \_\_\_\_\_

**TI-84+ GC 1: On/Off, 2<sup>nd</sup> functions, Screen, Batteries, Error Messages, Order of Operations**

Objectives: Find and use on and off, basic calculations, and 2<sup>nd</sup> functions  
 Raise and lower the brightness of the screen, use brightness to conserve batteries  
 Do multiple calculations at once using the order of operations  
 Recognize and respond to an error screen

In the lower left corner of the keypad:  turns the calculator on. On the casing, above the , is OFF. Notice what color the letters of OFF are. (Might be blue, green, or other) This color is above most buttons. Any time you want to use a function that's this color, press  (located in the upper left), then the key. To turn the calculator off, press  .

To make the screen brighter, press:  . You may have to do this more than once.

While you press  , notice that a number flashes in the upper-right corner of the screen. This number tells how high the brightness is. If it's too high, the screen will turn black.








To lower the brightness, press   as many times as needed (or hold it down).


Fresh batteries make brightness level 1 easy to read. Nearly dead batteries make brightness level 7 faint and hard to read.


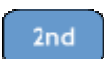

To use the batteries more slowly, lower the brightness as much as you can and still see easily. As your batteries fade, increase the brightness.


Check your brightness before every exam – if the brightness is high but the screen is faint, be sure to change the batteries or bring new batteries. You'll need four AAA batteries.

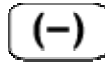
Numbers, decimal point, and common operations are at the bottom right of the keypad.

 is used as an equal sign. The key  (on the right side, above the divide symbol), called a "caret", is for exponents. (Caret  is not a directional key    .) Graphing calculators use the order of operations correctly, so you can put an entire expression into the calculator at once.

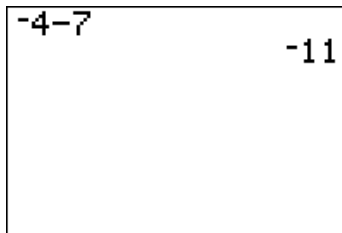
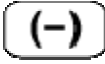
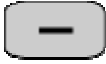
If you type something wrong, you can back up using the  key and type again.

Or you can delete using the  key, and insert using INS, which is  .

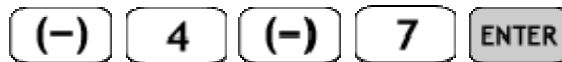
Or you can start over by pressing .

**TI-84+ GC 1: On/Off, 2<sup>nd</sup> functions, Screen, Batteries, Error Messages, Order of Operations**  
page 2means subtract.  
up or you'll get an error!

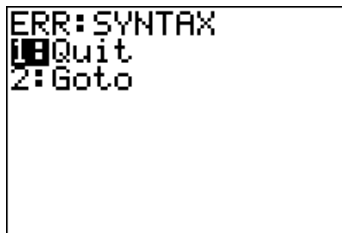
is used before a number to make it negative. Do not mix these

**Example 1:**  $-4 - 7 = -11$ Answer: -11Notice on your screen that the negative  is smaller and higher than the subtract .

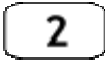
Try this calculation with a wrong key:

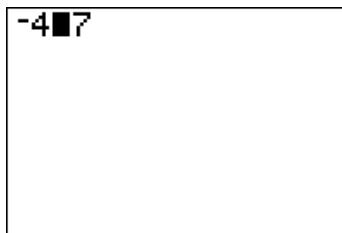


You'll get an error screen like this:




The calculator has several error screens. They all say "ERR:", an abbreviation for "Error", and then a word describing the type of error. "SYNTAX" means you typed something wrong. The next lines are a menu.

If you press  for "Goto", the calculator will go to the error by putting the cursor on the entry you typed wrong, like this:



You can type the correct key and press enter to get the correct calculation:



(If you press  for "Quit", it will exit the error menu without showing you the error.)

**TI-84+ GC 1: On/Off, 2<sup>nd</sup> functions, Screen, Batteries, Error Messages, Order of Operations**  
 page 3

Calculate two ways: with and without the calculator. If you don't get the same result, figure out why!

1)  $10.5 + 3(4) =$

{Remember: multiply before add.}

Answer: \_\_\_\_\_



2)  $-27 \div 3^2 =$

{Remember: exponents before divide.}

Answer: \_\_\_\_\_

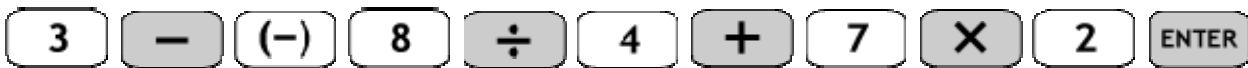


{That's a negative number, not subtract!}

3)  $3 - (-8) \div 4 + 7 \cdot 2$

{Remember: Subtract and add are the same priority, left to right, just as divide and multiply are the same priority, left to right.}

Answer: \_\_\_\_\_



4)  $(4 + 1)^3 \div 5$

{Remember: Grouping symbols before exponents.}

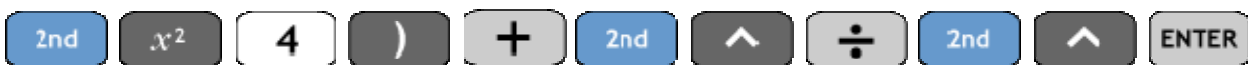
Answer: \_\_\_\_\_





5)  $\sqrt{4} + \frac{\pi}{\pi}$

{Remember: Any number divided by itself is 1.}

Answer: \_\_\_\_\_



{Notice the 2<sup>nd</sup> functions:  is square root and  is  $\pi$ . Also notice that the calculator opened a set of parentheses that you must close.}

**TI-84+ GC 1: On/Off, 2<sup>nd</sup> functions, Screen, Batteries, Error Messages, Order of Operations**  
page 4, Solutions


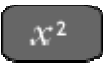
- 1) 22.5
- 2) -3
- 3) 19
- 4) 25
- 5) 3

Name \_\_\_\_\_

Date \_\_\_\_\_


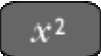

**TI-84+ GC 2: Exponents and Scientific Notation**

Objectives: Use the caret and square keys to calculate exponents  
 Review scientific notation  
 Input a calculation in scientific notation  
 Recognize an answer in scientific notation  
 Use scientific notation mode to display all results in scientific notation








The GC has two ways to do exponents. The caret key  can be used for any exponent by typing the base first, and then the caret and exponent. Because exponent 2 is used often, there's a shortcut key just for squaring: .

**Example 1:**  $2^3$ 




Answer: 8**Example 2:**  $3^2$ 



Answer: 9

Remember the order of operations: exponents before add, subtract, multiply or divide. If something should be added, subtracted, multiplied, or divided before the exponent, use parentheses.

**Example 3:**  $(3+4)^2$ 







Answer: 49**Example 4:**  $2^{(3+4)}$ 








Answer: 128

Remember also that any non-zero base raised to the zero power is 1.

**Example 5:**  $10^0$ 



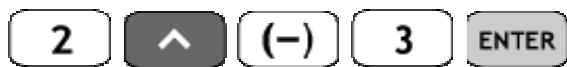


Answer: 1



Remember also that a negative exponent in the numerator is equivalent to a positive exponent in the denominator and a negative exponent in the denominator is equivalent to a positive exponent in the numerator.

**Example 6:**  $2^{-3} = \frac{1}{2^3} = \frac{1}{8}$



Answer: 0.125

**Example 7:**  $\frac{1}{3^{-2}} = 3^2$



Answer: 9

Recall: Scientific notation is a way of writing any number by using significant figures multiplied by a power of ten:  $a \times 10^b$ , where

$1 \leq a < 10$  (meaning that  $a$  has one nonzero digit to the left of the decimal point) and  $b$  is an integer  $\{\dots -3, -2, -1, 0, 1, 2, 3, \dots\}$ .

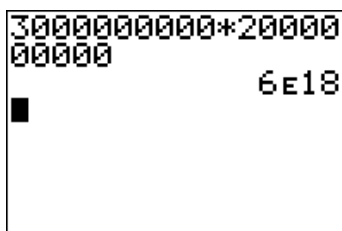
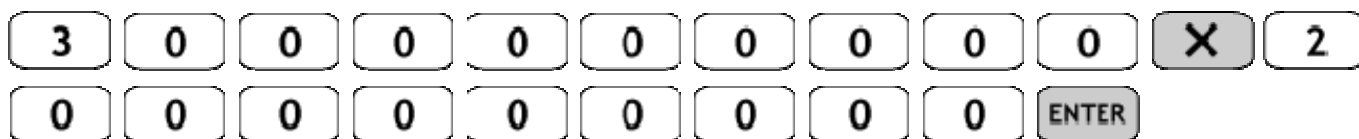
**Example 8:** 30,200 is written in scientific notation as  $3.02 \times 10^4$ .

**Example 9:** 0.0004087 is written in scientific notation as  $4.087 \times 10^{-4}$

**Example 10:** 3.901 is written in scientific notation as  $3.901 \times 10^0$


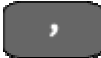
The GC automatically displays results in standard notation unless the result is a very large or very small number. Then it will automatically display the result in scientific notation.

**Example 11:**  $3,000,000,000 \times 2,000,000,000$



The GC uses its own abbreviation for scientific notation. **6E18** means  $6 \times 10^{18}$

**TI-84+ GC 2: Exponents and Scientific Notation** page 3

To input a number using scientific notation, use:  , the 2<sup>nd</sup> function EE which means 'multiply by a power of 10'. It appears as only E on the screen.

CAUTION: The notation E is not standard mathematical notation. Do not use it to write your final answers on papers or exams!


**Example 12:**  $3.02 \times 10^4$



3.02E4      30200

Answer: 30,200

To make the GC display all answers in scientific notation:

Press . Your screen changes to the MODE menu:

```
NORMAL SCI ENG
FLOAT 0 1 2 3 4 5 6 7 8 9
RADIAN DEGREE
FUNC PAR POL SEQ
CONNECTED DOT
SEQUENTIAL SIMUL
REAL a+bi Re*θi
FULL HORIZ G-T
SET CLOCK 08/10/10 1:56PM
```

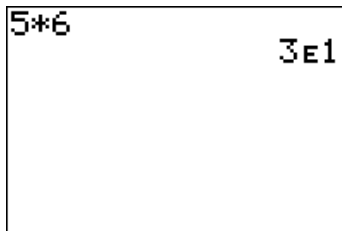
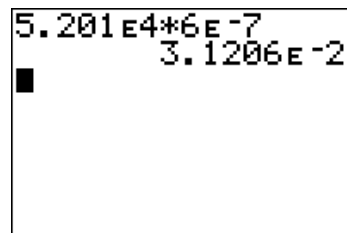
Each row of this screen is a menu. We'll only use the top row now.

When we select SCI, every result will be shown in scientific notation. This is sometimes very useful and sometimes not useful at all.

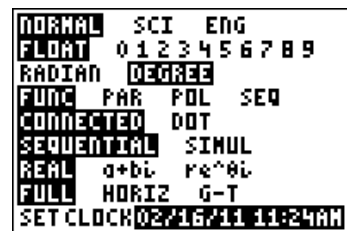
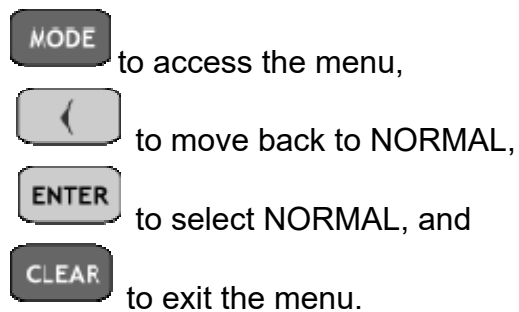
At the end of this exercise, we'll return to the NORMAL format.

Press  to move the shaded region from NORMAL to SCI and  to select SCI.

Then press   (or ) to QUIT the MODE menu.

**TI-84+ GC 2: Exponents and Scientific Notation** page 4**Example 13:** Write  $5 \times 6$  in scientific notation using GC in scientific notation mode.Answer:  $3 \times 10^1$ **Example 14:** Write  $(5.201 \times 10^4)(6 \times 10^{-7})$  in scientific notation using GC in scientific notation mode.Answer:  $3.1206 \times 10^{-2}$ 

To leave scientific notation mode and return to normal mode, press:



**TI-84+ GC 2: Exponents and Scientific Notation** page 5

Practice:

1)  $(-9)^2$  {Negative before exponent.}

Answer: \_\_\_\_\_

2)  $-9^2$  {Exponent before negative.}

Answer: \_\_\_\_\_

3)  $\frac{3^2}{4}$  {Exponent before divide.}

Answer: \_\_\_\_\_

4)  $\left(\frac{3}{4}\right)^2$  {Divide before exponent.}

Answer: \_\_\_\_\_

Write result in scientific notation.

5)  $300,000,000,000,000,000,000 \times 7,000,000,000,000,000,000,000,000$

Answer: \_\_\_\_\_

6)  $0.000000000005 \times 0.0000000000002$

Answer: \_\_\_\_\_

Write in standard notation by using your GC in standard display mode.

7)  $3 \times 10^5$

Answer: \_\_\_\_\_

8)  $2.116 \times 10^{-3}$

Answer: \_\_\_\_\_

9)  $6,000 \times 700,000$

Answer: \_\_\_\_\_

10)  $0.000008 \times 0.000000003$

Answer: \_\_\_\_\_

Write in scientific notation by using the GC in scientific notation mode.

11)  $0.36 \times 9$

Answer: \_\_\_\_\_

12)  $0.025 \div 0.5$

Answer: \_\_\_\_\_

13)  $0.00000008 \times 90,000,000$

Answer: \_\_\_\_\_

14)  $\frac{0.00000000000008}{40,000,000,000,000}$

Answer: \_\_\_\_\_

15)  $\frac{6,000,000,000,000}{0.0000002}$

Answer: \_\_\_\_\_

16)  $\frac{0.0000000008}{0.002}$

Answer: \_\_\_\_\_

17)  $\frac{7000000000}{5000000}$

Answer: \_\_\_\_\_

**TI-84+ GC 2: Exponents and Scientific Notation** page 6 Solutions

1) 81

2) -81

3) 2.25

4) 0.5625

5)  $(3 \times 10^{23})(7 \times 10^{30}) = 2.1 \times 10^{54}$

6)  $(5 \times 10^{-11})(2 \times 10^{-13}) = 1 \times 10^{-23}$

7)  $3 \times 10^5 = 300,000$

8)  $2.116 \times 10^{-3} = 0.002116$

9)  $(6 \times 10^3)(7 \times 10^5) = 4.2 \times 10^9 = 4,200,000,000$

10)  $2.4 \times 10^{-13} = 0.000000000000024$

11)  $3.24 \times 10^0 = 3.24$

12)  $5 \times 10^{-2} = 0.05$

13)  $7.2 = 7.2 \times 10^0$

14)  $\frac{(8 \times 10^{-14})}{(4 \times 10^{13})} = 2 \times 10^{-27}$

15)  $\frac{(6 \times 10^{12})}{(2 \times 10^{-12})} = 3 \times 10^{24}$

16)  $\frac{(8 \times 10^{-9})}{(2 \times 10^{-3})} = 4 \times 10^{-6} = 0.000004$

17)  $\frac{7 \times 10^9}{5 \times 10^7} = 1.4 \times 10^2 = 140$

Name \_\_\_\_\_

Date \_\_\_\_\_

**TI-84+ GC 3: Order of Operations, Additional Parentheses, Roots and Absolute Value**

Objectives: Review the order of operations  
 Observe that the GC uses the order of operations  
 Use parentheses in GC commands to achieve correct calculations  
 Calculate 3<sup>rd</sup>, 4<sup>th</sup>, or other roots using the MATH menu  
 Calculate absolute value using the MATH menu

The order of operations is a list of rules about the order we do the parts of a calculation containing several parts. Some sources use the acronym PEMDAS. Graphing calculators have been programmed to follow the order of operations.

Step 1: Identify all grouping symbols and resolve them from the inside out. Grouping symbols include purely grouping symbols and grouping symbols which are also operators.

Parentheses ( ), Brackets [ ], and Braces { } -- grouping only

Fraction bars – horizontal line creates numerator and denominator groups before divide

For example:  $\frac{2-3}{7-4}$  means  $(2-3) \div (7-4)$ .

Square Roots and other radicals: The radical symbol may enclose a group, before root

For example:  $\sqrt{2 \cdot 3 + 8}$  means  $\sqrt{(2 \cdot 3 + 8)}$

Absolute values: The vertical bars may enclose a group, before absolute value

For example:  $|3 - 17 \cdot 2|$  means  $|(3 - 17 \cdot 2)|$

Step 2: **E**xponents, roots, radicals. Work from left to right.

Step 3: **M**ultiply and **D**ivide. Work from left to right. Divide may come before multiply.

Step 4: **A**dd and **S**ubtract. Work from left to right. Subtract may come before add.

**Example 1:**  $5 - 3 + 1$



Answer: 3

The GC does not have keys for brackets [ ] or braces { } as grouping symbols. So use parenthesis keys for all of these symbols, nesting if necessary.

Note: You must have the same number of open  as you have closed  parentheses.

**Example 2:**  $\{3 - [4 + 7(1 - 5)]\}$

( 3 - ( 4 + 7 ( 1 - 5 ) ) )

(3-(4+7(1-5)))

27

) ) ENTER

Notice: three open, three closed.  
Answer: 27

If a fraction bar appears in the problem, we must add parentheses around the numerator group and around the denominator group when we calculate on the GC.

**Example 3:**  $\frac{25-19}{14-17}$  becomes  $\frac{(25-19)}{(14-17)}$

( 2 5 - 1 9 ) ÷ ( 1 4 - )

(25-19)/(14-17)

-2

1 7 ) ENTER

Answer: -2

Recall: the square root is a 2<sup>nd</sup> function, above the  $x^2$  key.

Caution: When calculating square roots, the TI-84+ will open the first parenthesis for you. But you will have to remember to close that set of parentheses.

**Example 4:**  $\sqrt{1+3 \cdot 5}$  becomes  $\sqrt{(1+3 \cdot 5)}$

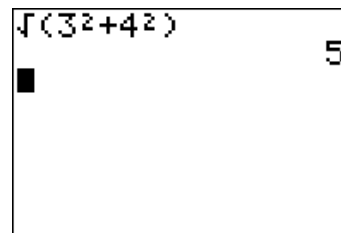
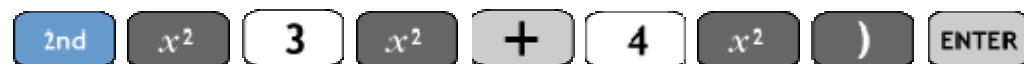
2nd  $x^2$  1 + 3 × 5 ) ENTER

√(1+3\*5)

4

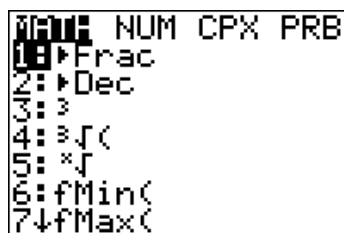
Answer: 4

**Example 5:**  $\sqrt{3^2 + 4^2}$  becomes  $\sqrt{(3^2 + 4^2)}$



Answer: 5

To calculate 3<sup>rd</sup>, 4<sup>th</sup>, or higher roots, use the **MATH** button, which opens a screen with four menus across the top: MATH, NUM, CPX, and PRB. You are automatically in the MATH menu, which is highlighted. We will use the NUM menu later.

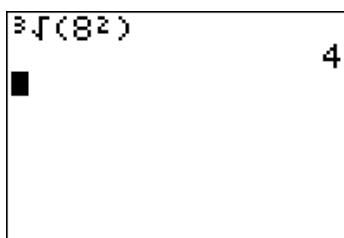


Notice that the 4<sup>th</sup> option in the MATH menu is  $\sqrt[3]{\phantom{x}}$ . Select this option one of two ways:

One way is to use the down arrow to move to 4:, then press .

A quicker way is to press (at any time in this window) to select option 4.

**Example 6:**  $\sqrt[3]{8^2}$

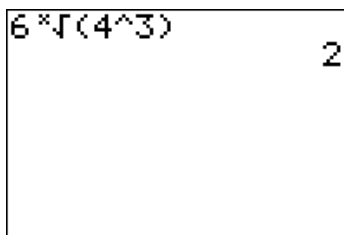
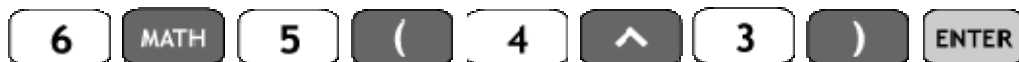


Answer: 4

To calculate higher-order roots, we use the MATH menu again, but select option 5. Caution: Option 5 uses “x” to show the type of root. We need to type this number before we use the MATH menu. Also note: this does not open parentheses, so we have to open them.



Example 7:  $\sqrt[6]{4^3}$

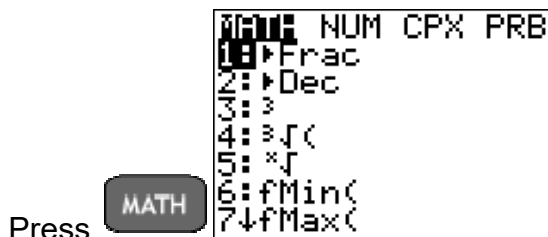


Answer: 2

Important facts about absolute value:

1. Absolute value returns a non-negative answer.
2. Absolute value is a grouping symbol. When evaluating, completely resolve the inside first.
3.  $|x|$  and  $x$  are not the same. A variable  $x$  can represent a positive, negative, or zero, but  $|x|$  can't be negative. We cannot ignore or "remove" the absolute value.

To calculate absolute value, we use the MATH button again, but also move to the second menu, NUM (for number).



Press



Press



for the NUM menu:

Press **1** or **ENTER** to select absolute value, abbreviated abs(

Caution: The GC absolute value opens parentheses. If you do not close them, the GC will take the absolute value of the entire expression.

**Example 8:**  $|-2|$ 

MATH  $\rightarrow$  1  $(-)$  2  $)$  ENTER

```
abs(-2)
2
```

Answer: 2**Example 9:**  $|5|$ 

MATH  $\rightarrow$  ENTER 5 ENTER

```
abs(5
5
```

Answer: 5**Example 10:**  $|0|$ 

MATH  $\rightarrow$  ENTER 0 ENTER

```
abs(0
0
```

Answer: 0**Example 11:**  $|-2 + 3(-8)|$ 

MATH  $\rightarrow$  ENTER  $(-)$  2  $+$  3  $\times$   $(-)$  8  $)$  ENTER

```
abs(-2+3*-8)
26
```

Answer: 26**Example 12:**  $|-2| + 3(-8)$ 

MATH  $\rightarrow$  ENTER  $(-)$  2  $)$   $+$  3  $\times$   $(-)$  8 ENTER

```
abs(-2)+3*-8
-22
```

Answer: -22

Practice:

Calculate. Write the keystrokes you use in the blank boxes. Check by doing the problem yourself.

1)  $5 - (3 + 1)$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

2)  $12 \cdot 4 + 3$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

3)  $12 \cdot (4 + 3)$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

4)  $12 - 9 \div 3 \cdot 6 \div 2 - 3$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

5)  $9 - 12 \div 4 - 8$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

6)  $2^3$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

7)  $3^2$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

8)  $2 + 3^2$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

9)  $(2 + 3)^2$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

10)  $9 - 12 \div (4 - 6)$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

11)  $(9 - 12) \div (4 - 6)$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

12)  $9 - 12 \div 4 - 6^2$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

13)  $(9 - 12) \div (4 - 6)^2$

Answer: \_\_\_\_\_


14)  $18 \div 6 \times 2 - 3 + 9$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

15)  $\{3 - [4 + 7(1 - 5)^2]\}$

Answer: \_\_\_\_\_


16)  $\frac{9 - 12}{4 - 6}$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

17)  $\frac{3^2 - 2^2}{3 \cdot 2 + 2^2}$

Answer: \_\_\_\_\_


18)  $\frac{(-2)^2 + 1}{-2 - 3}$

Answer: \_\_\_\_\_


$$19) \frac{-2^2 + 1}{-2 - 3}$$

Answer: \_\_\_\_\_


$$20) (-2)^2 + \frac{1}{-2} - 3$$

Answer: \_\_\_\_\_


$$21) -2^2 + \frac{1}{-2} - 3$$

Answer: \_\_\_\_\_


$$22) (-2)^2 + \frac{1}{-2 - 3}$$

Answer: \_\_\_\_\_


$$23) -2^2 + \frac{1}{-2 - 3}$$

Answer: \_\_\_\_\_


$$24) \frac{(-2)^2 + 1}{-2} - 3$$

Answer: \_\_\_\_\_


25)  $\frac{-2^2 + 1}{-2} - 3$

Answer: \_\_\_\_\_


26)  $\frac{(-2+1)^2}{-2} - 3$

Answer: \_\_\_\_\_


27)  $\frac{(-2+1)^2}{-2-3}$

Answer: \_\_\_\_\_


28)  $\sqrt{6^2 + 8^2}$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

29)  $\sqrt[3]{5+120}$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

30)  $\sqrt[5]{32}$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

31)  $\sqrt[4]{5^3 + 5(10^2)}$

Answer: \_\_\_\_\_


**TI-84+ GC 3: Order of Operations, Additional Parentheses, Roots and Absolute Value**  
 page 10

32)  $|7 + -3(5)|$

Answer: \_\_\_\_\_

--	--	--	--	--	--	--	--	--	--	--	--	--

33)  $|-1(12)| - 3|-2|$

Answer: \_\_\_\_\_


34)  $\frac{-3 + 6}{|2 - 7| - |-2|}$

Answer: \_\_\_\_\_


35)  $\frac{2 + 3|5 - (-1)|}{11 + 2(-3)}$

Answer: \_\_\_\_\_


36)  $\frac{|7 - 11|}{|4 - 8|} - \frac{2|23 - 19|}{|-3 - 1|}$

Answer: \_\_\_\_\_


37)  $\frac{|17 - 5|}{2 - 5}$

Answer: \_\_\_\_\_


**TI-84+ GC 3: Order of Operations, Additional Parentheses, Roots and Absolute Value**  
 page 11

Solutions:

1) 1                      5) -2

2) 51                    6) 8

3) 84                    7) 9

4) 0                     8) 11

9) 25

13) -0.75

10) 15

14) 12

11) 1.5

12) -30

15) -113

$$\frac{(3-(4+7(1-5)^2))}{-113}$$

20) 0.5

$$\frac{(-2)^2+1}{-2-3} .5$$

16) 1.5

$$\frac{(9-12)/(4-6)}{1.5}$$

21) -7.5

$$\frac{-2^2+1}{-2-3} -7.5$$

17) .5

$$\frac{(3^2-2^2)/(3*2+2^2)}{.5}$$

22) 3.8

$$\frac{(-2)^2+1/(-2-3)}{3.8}$$

18) -1

$$\frac{((-2)^2+1)/(-2-3)}{-1}$$

23) -4.2

$$\frac{-2^2+1/(-2-3)}{-4.2}$$

19) 0.6

$$\frac{(-2^2+1)/(-2-3)}{.6}$$

24) -5.5

$$\frac{((-2)^2+1)/-2-3}{-5.5}$$



**TI-84+ GC 3: Order of Operations, Additional Parentheses, Roots and Absolute Value**  
 page 12

25) 
$$\frac{(-2^2+1)/-2-3}{-1.5}$$

26) 
$$\frac{(-2+1)^2/-2-3}{-3.5}$$

27) 
$$\frac{(-2+1)^2/(-2-3)}{-0.2}$$

28) 
$$\sqrt{6^2+8^2}$$

29) 
$$\sqrt[3]{5+120}$$

30) 
$$5 \cdot \sqrt{32}$$

31) 
$$4 \cdot \sqrt{5^3+5(10^2)}$$

32) 
$$\text{abs}(7+ -3 \cdot 5)$$

33) 
$$\frac{\text{abs}(-1 \cdot 12) - 3 \cdot \text{abs}(-2)}{6}$$

34) 
$$\frac{(-3+6)/(\text{abs}(2-7))}{-\text{abs}(-2)}$$

35) 
$$\frac{(2+3 \cdot \text{abs}(5- -1))/(-11+2 \cdot -3)}{4}$$

36) 
$$\frac{\text{abs}(7-11)/\text{abs}(4-8) - 2 \cdot \text{abs}(23-19)/\text{abs}(-3-1)}{-1}$$

37) 
$$\frac{\text{abs}((17-5)/(2-5))}{4}$$

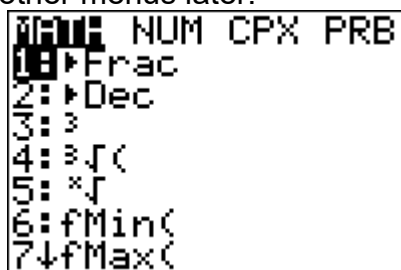
Name \_\_\_\_\_

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**TI-84+ GC 4 Fractions, Decimals, Rational and Irrational Numbers**




Objectives: Convert decimals to fractions on the GC, where possible  
 Use the 2<sup>nd</sup> function ANS to recall the previous GC result and continue  
 Review rational and irrational numbers  
 Understand the limitations of the GC's fraction capacity  
 Use >frac in calculations



The **MATH** button on your calculator opens a screen with four menus across the top: MATH, NUM, CPX, and PRB. You are automatically in the MATH menu, which is highlighted. We may use other menus later.



```

MATH NUM CPX PRB
1: >Frac
2: >Dec
3: 3
4: >√(
5: *√
6: fMin(
7: fMax(
  
```

Each option in any menu is numbered. To use options in any menu, move with the  or  until the desired option number is highlighted, then press . Or, you can select an option by typing its number. When you open a menu, the first option is automatically highlighted.

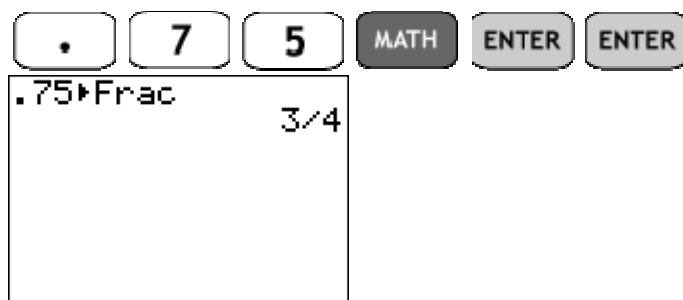
Pressing **MATH**  will select option 1, >FRAC. Press  again to find the fraction.

Remember: A rational number is a number that can be written as a fraction (or ratio) of two integers.

In the MATH menu, option 1, >FRAC will convert an existing answer to a fraction, if

- the decimal is a rational number AND
- the decimal is in the calculator's database of fractions

**Example 1:** Convert .75 to a fraction.



.75 >Frac  $\frac{3}{4}$

Answer:  $\frac{3}{4}$

**TI-84+ GC 4 Fractions, Decimals, Rational and Irrational Numbers, page 2**



**Example 2:** Calculate and convert to fraction using the GC:  $\frac{2}{3} + \frac{7}{11}$



2/3+7/11►Frac  
43/33

Answer:  $\frac{43}{33}$

The GC temporarily keeps the value of your last calculation in a special memory location called Answer. If you mistakenly press ENTER before converting it to a fraction, you can retrieve the

answer and keep going by using Answer, ANS, which is  .

Sometimes you can type the operation, and the GC will automatically insert Ans for you.

**Example 3:** (calculation, but forget to convert to fraction)  $\frac{1}{2} + \frac{5}{6}$



Answer:  $1.\bar{3}$

**Example 4:** (recall previous answer and convert to fraction)

Recall previous answer:   Convert to fraction   

1/2+5/6  
1.333333333  
Ans►Frac  
4/3

Answer:  $\frac{4}{3}$

Recall: Irrational numbers cannot be written as a fraction of two integers.  
("ir" means "not", so "ir" + "rational" = "not rational")

**Example 5:**  $\sqrt{2}$  is irrational, and so it cannot be written as a fraction of two integers.




**Example 6:**  $\pi$  is irrational, and so it cannot be written as a fraction of two integers.

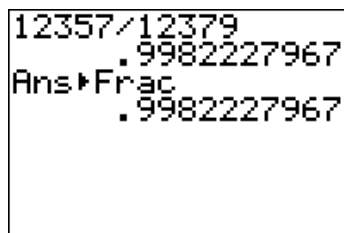
Sometimes >Frac does not give a fraction answer. There are two reasons why this happens.

1. The number you typed is irrational (not a rational number) and cannot be written as a fraction. In this case, you need to use your brain to recognize irrational numbers.
2. The number can be written as a fraction, but it's not a fraction in the GC's database. In this case, you need to use your brain to recognize rational numbers. See Example 7.

**CAUTION:** You cannot tell from your calculator if the decimal is a rational number that's not in the database or if the decimal is a rounded irrational number. In either case, the GC will return the approximate decimal. You must know whether it's a rational or irrational answer!

**Example 7:** Calculate the fraction  $\frac{12357}{12379}$  as a decimal. Then ask the GC to convert it to fraction.

Calculate the decimal by dividing   then convert to fraction 

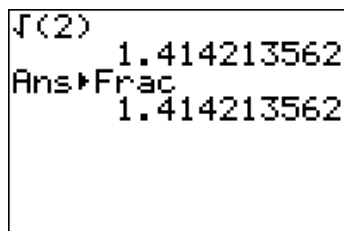


Answer: The fraction is  $\frac{12357}{12379}$ , but we know it from thinking, not by GC.

The fraction  $\frac{12357}{12379}$  is not in the GC database of fractions and decimal equivalents.

**Example 8:** Calculate  $\sqrt{2}$  and attempt to convert it to fraction.

Calculate  $\sqrt{2}$ :    
 Attempt to convert to fraction: 



Answer:  $\sqrt{2}$  cannot be written as a fraction, no matter who's trying. It's irrational.

**Example 9:** Calculate  $\frac{2}{3} - \pi + \frac{4}{5}(9)$  exactly.

Wrong method: The entire calculation, with the  $\pi$  and without thinking:



```
2/3-π+4/5*9
4.725074013
Ans▶Frac
4.725074013
█
```

Because there's a  $\pi$  in the expression, it's irrational.

Correct method:

Simplify the other fractions that do not contain  $\pi$ :



```
2/3-π+4/5*9
4.725074013
Ans▶Frac
4.725074013
2/3+4/5*9▶Frac
118/15
```

Then subtract with common denominator (by hand) to get a single fraction:

$$\frac{118}{15} - \pi = \frac{118}{15} - \frac{15\pi}{15} = \frac{118 - 15\pi}{15}$$

Answer: Irrational

Answer:  $\frac{118 - 15\pi}{15}$

**TI-84+ GC 4 Fractions, Decimals, Rational and Irrational Numbers, page 5**

Practice: Calculate and convert to fraction. If the GC gives a fraction, write the fraction. Identify if the result is rational or irrational. If the GC did not give a fraction, find the exact answer.

$$1) \frac{1}{3} + \frac{7}{8} \left( \frac{5}{6} - \frac{1}{9} \right)$$

Circle: Rational – Irrational

Answer: \_\_\_\_\_

$$2) 3 \left( \frac{5}{7} - \frac{1}{3} \cdot \frac{8}{9} \right)$$

Circle: Rational – Irrational

Answer: \_\_\_\_\_

$$3) \frac{\frac{1}{5} - \frac{2}{7}}{\frac{5}{4} + \frac{3}{8}}$$

Circle: Rational – Irrational

Answer: \_\_\_\_\_

$$4) \left( \frac{4}{9} \right)^2 - \left( \frac{2}{5} \right)^2$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$5) 0.002 - 75(0.025)$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$6) \frac{2}{3} - 7.25 + \frac{4}{5}(9)$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$7) \frac{4^2}{9} - \frac{2^3}{5}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$8) \frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{3} + \frac{\sqrt{4}}{4}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$9) \frac{2079}{2081} + \frac{1}{2081}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$10) \frac{\sqrt{9}}{2} + \frac{\sqrt{16}}{3} + \frac{\sqrt{4}}{4}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$11) \frac{316}{79} \cdot \frac{367}{2213} + \frac{743}{2213}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$12) \frac{2}{2014} - \frac{1}{4028}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$13) \frac{\pi}{3} - \frac{\pi}{6}$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

$$14) \frac{\pi}{4} + 3 \left( \frac{\pi}{8} \right)$$

Circle: Rational - Irrational

Answer: \_\_\_\_\_

**TI-84+ GC 4 Fractions, Decimals, Rational and Irrational Numbers, page 6**

Practice: Calculate. Give integer or fraction answers, not decimals.

15) 
$$\frac{|2-9| - |-8|}{-6}$$

Answer: \_\_\_\_\_


16) 
$$\frac{4(-5+2)}{3} - \frac{-5(3-8)}{6-(-7)}$$

Answer: \_\_\_\_\_


17) 
$$\frac{-3\sqrt{60+4} + (-3)^2}{2^3 + |4(-7)|}$$

Answer: \_\_\_\_\_


18) 
$$\frac{(-3)^4 + 4\sqrt{125-44}}{5^2 + |6(-3)|}$$

Answer: \_\_\_\_\_


19) 
$$\frac{\frac{1}{4} \cdot 15 - 3}{7 + \frac{1}{3} \cdot 8}$$

Answer: \_\_\_\_\_


Solutions:

1)

Calculator display showing the expression  $\frac{1}{3} + 7 \div 8 \times (5 \div 6 - 1 \div 9)$  and the result  $139/144$ .

Rational, Answer:  $\frac{139}{144}$

2)

Calculator display showing the expression  $3(5/7 - 1/3 \times 8/9)$  and the result  $79/63$ .

Rational, Answer:  $\frac{79}{63}$

3)

Calculator display showing the expression  $(1/5 - 2/7) \div (5/4 + 3/8)$  and the result  $-24/455$ .

Rational, Answer:  $-\frac{24}{455}$

4)

Calculator display showing the expression  $(4/9)^2 - (2/5)^2$  and the result  $76/2025$ .

Rational, Answer:  $\frac{76}{2025}$

5)

Calculator display showing the expression  $.002 - 75 \times .025$  and the result  $-1873/1000$ .

Rational, Answer:  $-\frac{1873}{1000}$



**TI-84+ GC 4 Fractions, Decimals, Rational and Irrational Numbers, page 8 Solutions**

6)

Rational, Answer:  $\frac{37}{60}$

7)

Rational, Answer:  $\frac{8}{45}$

8) Irrational,  $\frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{3} + \frac{\sqrt{4}}{4} = \frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{3} + \frac{2}{4} =$   
 $\frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{3} + \frac{1}{2} = \frac{3\sqrt{2}}{6} + \frac{2\sqrt{3}}{6} + \frac{3}{6} = \text{Ans:}$   
 $\frac{3\sqrt{2} + 2\sqrt{3} + 3}{6}$

9) Rational,  $\frac{2079}{2081} + \frac{1}{2081} = \text{Answer: } \frac{2080}{2081}$

10)

Rational,  
 Answer:  $\frac{10}{3}$

11) Rational,  $\frac{316}{79} \cdot \frac{367}{2213} + \frac{743}{2213} =$   
 $4 \cdot \frac{367}{2213} + \frac{743}{2213} = \frac{1468}{2213} + \frac{743}{2213} = \text{Answer:}$   
 $\frac{2211}{2213}$

12) Rational,  $\frac{2}{2014} - \frac{1}{4028} = \frac{4}{4028} - \frac{1}{4028} =$   
 Answer:  $\frac{3}{4028}$

13) Irrational,  $\frac{\pi}{3} - \frac{\pi}{6} = \frac{2\pi}{6} - \frac{\pi}{6} = \text{Answer:}$   
 $\frac{\pi}{6}$

14) Irrational,  $\frac{\pi}{4} + 3\left(\frac{\pi}{8}\right) = \frac{2\pi}{8} + \frac{3\pi}{8} =$   
 Answer:  $\frac{5\pi}{8}$

**TI-84+ GC 4 Fractions, Decimals, Rational and Irrational Numbers, page 9 Solutions**

15)  $\frac{1}{6}$

```
(abs(2-9)-abs(-8
))/-6
.1666666667
Ans►Frac
1/6
```

16)  $-\frac{77}{13}$

```
4(-5+2)/3-5(3-8
)/(6--7)
-5.923076923
Ans►Frac
-77/13
```

17)  $-\frac{5}{12}$

```
(-3*J(60+4)+(-3)
^2)/(2^3+abs(4*(-
7)))
-.4166666667
Ans►Frac
-5/12
```

18)  $\frac{117}{34}$

```
((-3)^4+4*J(125-
44))/(5^2+abs(6--
3))
3.441176471
Ans►Frac
117/34
```

19)  $\frac{9}{116}$

```
(1/4*15-3)/(7+1/
3*8)
.0775862069
Ans►Frac
9/116
```

Name \_\_\_\_\_

Date \_\_\_\_\_

**TI-84+ GC 6 Exact vs. Approximate Results with Fractions and Decimals**

**Objectives**    Learn the meaning of “exact” and “approximate”  
                       Use exact forms and approximate forms of fractions correctly  
                       Recognize that the GC display can be an approximate answer

An exact answer has no error. If we use an exact result to perform additional calculations, we'll continue to get exactly the right answer. If we perform the same calculation to different versions of an exact answer, we'll always get the same, exact final result. We use the symbol = to show that the result is exactly equal.

An approximate answer is close to the exact answer, but is a “near miss”. We usually find approximate answers by rounding or approximating. If we start with an approximate answer and perform additional calculations, we'll get approximate final results. We use the symbol  $\approx$  to show that the result is approximately equal.

**CAUTION:** You should always give an EXACT answer unless the instructions tell you to round.

**Example 1:** Write the number  $\frac{9}{7}$  several ways and identify if each is exact or approximate.

Exact answers:  $\frac{9}{7} = 1\frac{2}{7} = 1.\overline{285714}$

Approximate answers:  $\frac{9}{7} \approx 1.29$ ,  $\frac{9}{7} \approx 1.285714$ ,  $\frac{9}{7} \approx 1.285714286$

<b>Exact Answers</b>	<b>Should I do this?</b>
Improper Fraction $\frac{9}{7}$	Yes. An improper fraction is exact, and usually easier for continuing calculations.
Terminating decimal, with all places (Does not apply to this example.)	Maybe. If the decimal is short, yes. If the decimal is longer, probably not, since you may copy or type it wrong.
Mixed Number $1\frac{2}{7}$	Maybe. A mixed number is exact, but is often annoying for calculations.
Decimal with repeat bar $1.\overline{285714}$	Probably not. This is an exact answer, but it's not always easy to find or use.

<b>Approximate Answers</b>	<b>Should I do this?</b>
Rounded decimal: 1.29 or 1.285714 or rounded to any place value	Probably not. Read the instructions. Only round if the instructions say to round, and only round to the place instructed.
All decimal places in calculator screen for a non-terminating decimal: 1.285714286	NEVER. The calculator has rounded this answer so it will fit on the screen.

<b>Wrong Answers</b>	<b>Should I do this?</b>
Incorrectly rounded decimal: 1.28 (chopped)	Never.

**TI-84+ GC 6: Exact vs. Approximate Results with Fractions and Decimals**, page 2

The calculator shows all the places its “brain” can comprehend. But its “brain” only has 9-15 decimal places, which is not always enough.

**Example 2:** Calculate several answers for  $\frac{9}{7} \cdot 7$  and identify if each is exact or approximate.

a.  $\frac{9}{7} \cdot 7$

Answer: 9, exact

b.  $\left(1\frac{2}{7}\right) \cdot 7$

Answer: 9, exact

c.  $(1.29) \cdot 7$

Answer:  $\approx 9.03$ , approximate

d.  $(1.285714) \cdot 7$

Answer:  $\approx 8.999998$ , approximate

e.  $(1.285714286) \cdot 7$

Answer:  $\approx 9.000000002$ , approximate

(retype the decimal, don't use ANS)

f. If your exam question asks you to find  $\frac{9}{7} \cdot 7$ , which answer(s) would be correct?

Answer: Only the exact answer 9 (obtained from a or b) is correct.

**Example 3:** Calculate different answers for  $\frac{7}{9} \cdot 36$  and identify if each is exact or approximate.

a.  $\frac{7}{9} \cdot 36 = 28$  exact

b.  $(.777777778) \cdot 36 = 28.00000001$  is approximately equal to  $\frac{7}{9} \cdot 36$

So far, so good. But do these next two by hand first, then use your GC.

c.  $(.7777777778) \cdot 36 = 28.0000000008$  is approximately equal to  $\frac{7}{9} \cdot 36$

d.  $(.7777777777) \cdot 36 = 27.9999999972$  is approximately equal to  $\frac{7}{9} \cdot 36$

For both of these, the GC gives 28 because it rounded when its “brain” was too small.

**TI-84+ GC 6: Exact vs. Approximate Results with Fractions and Decimals**, page 3

Practice: Perform the calculations and identify if your answers are exact or approximate.

- 1) Write  $\frac{7}{9}$  as a decimal. \_\_\_\_\_ Exact or approximate?
  - a. Round to the nearest ten-thousandth: \_\_\_\_\_ Exact or approximate?
  - b. Every decimal place on the calculator: \_\_\_\_\_ Exact or approximate?
- 2) Write  $\frac{1}{3}$  as a decimal. \_\_\_\_\_ Exact or approximate?
  - a. Round to the nearest thousandth: \_\_\_\_\_ Exact or approximate?
  - b. Every decimal place on the calculator: \_\_\_\_\_ Exact or approximate?
- 3) Give several different answers for  $\frac{1}{3} \cdot 9$ .
  - a.  $\frac{1}{3} \cdot 9 =$  \_\_\_\_\_ Exact or approximate?
  - b.  $(0.333) \cdot 9 =$  \_\_\_\_\_ Exactly or approximately equal to  $\frac{1}{3} \cdot 9$ ?
  - c.  $(0.333333333) \cdot 9 =$  \_\_\_\_\_ Exactly or approximately equal to  $\frac{1}{3} \cdot 9$ ?
  - d. If your exam question asks you to find  $\frac{1}{3} \cdot 9$ , which answer(s) would be correct?
- 4) Write  $\frac{7}{8}$  as a decimal. \_\_\_\_\_ Exact or approximate?
  - a. Round to the nearest hundredth: \_\_\_\_\_ Exact or approximate?
  - b. Round to the nearest tenth: \_\_\_\_\_ Exact or approximate?
- 5) Calculate different answers for  $\frac{7}{8} \cdot 16$  and identify if exact or approximate.
  - a.  $\frac{7}{8} \cdot 16 =$  \_\_\_\_\_ Exact or approximate?
  - b.  $(0.875) \cdot 16 =$  \_\_\_\_\_ Exactly or approximately equal to  $\frac{7}{8} \cdot 16$ ?
  - c.  $(0.88) \cdot 16 =$  \_\_\_\_\_ Exactly or approximately equal to  $\frac{7}{8} \cdot 16$ ?
  - d.  $(0.9) \cdot 16 =$  \_\_\_\_\_ Exactly or approximately equal to  $\frac{7}{8} \cdot 16$ ?
  - e. If your exam question asks you to find  $\frac{7}{8} \cdot 16$ , which answer(s) would be correct?

**TI-84+ GC 6: Exact vs. Approximate Results with Fractions and Decimals**, solutions, page 4

1)  $\frac{7}{9} = 0.\overline{7}$ , a repeating decimal or fraction is exact.

a.  $\frac{7}{9} \approx 0.7778$  approximate

b.  $\frac{7}{9} \approx 0.7777777778$  approximate

2)  $\frac{1}{3} = 0.\overline{3}$ , repeating decimal, exact (must use repeat bar).

a.  $\frac{1}{3} \approx 0.333$  approximate

b.  $\frac{1}{3} \approx 0.3333333333$  approximate

3) a.  $\frac{1}{3} \cdot 9 = 3$  exact

b.  $\frac{1}{3} \cdot 9 \approx 2.997$  approximate

c.  $\frac{1}{3} \cdot 9 \approx 2.999999997$  approximate

d. Only the exact answer 3, obtained from a, would be correct.

4)  $\frac{7}{8} = 0.875$  exact

a.  $\frac{7}{8} \approx 0.88$  approximate

b.  $\frac{7}{8} \approx 0.9$  approximate

5) a.  $\frac{7}{8} \cdot 16 = 14$  exact

b.  $\frac{7}{8} \cdot 16 = 0.875 \cdot 16 = 14$  exact

c.  $\frac{7}{8} \cdot 16 \approx 14.08$  approximate

d.  $\frac{7}{8} \cdot 16 \approx 14.4$  approximate

e. Only the exact answer 14, obtained from a. or b. would be correct.


Name \_\_\_\_\_

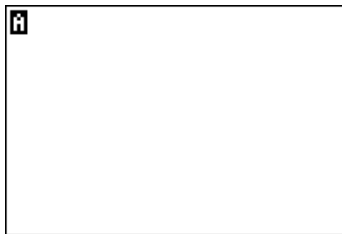
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**TI-84+ GC 5 Memory Locations and Editing Using Answer, Entry, Delete, and Insert**

- Objectives: Use memory locations for repeated calculations with different variables  
 Use the GC's automatic recall of the previous answer, ANS  
 Recall a previous calculation using Entry (ENTRY = 2<sup>nd</sup> ENTER)  
 Edit a previous calculation using Delete (DEL) and Insert (INS = 2<sup>nd</sup> DEL)

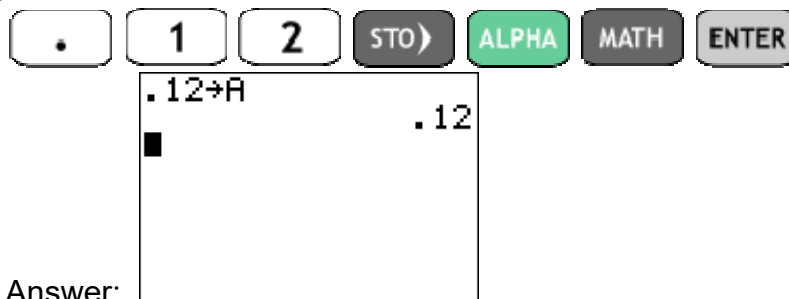
The GC has the ability to store numbers in memory so that they can be used again later. Memory locations are letters A through Z, which we access using the ALPHA button in the upper-left under the 2<sup>nd</sup> key. Usually the ALPHA button is the same color as the letters A through Z, which appear above your regular GC buttons next to the 2<sup>nd</sup> functions.

Notice after you press the ALPHA  key, the GC cursor changes to the letter A to indicate that your next keystroke will be an alphabetical memory location.  
 (If you pressed ALPHA by mistake, press it again to return the cursor to normal.)

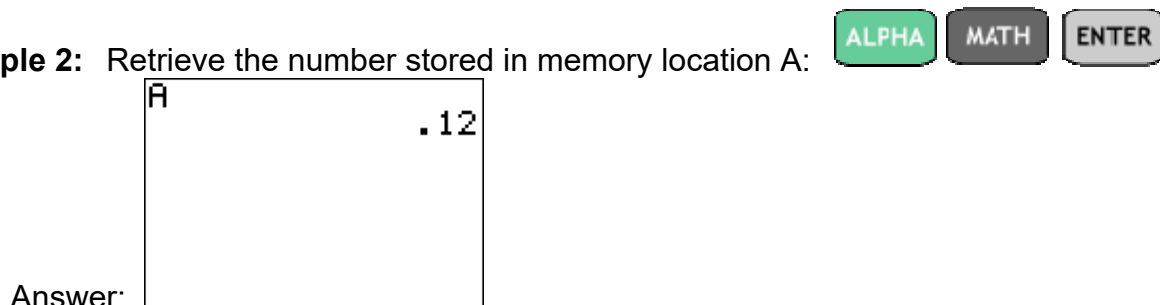


To store a number in memory, type or calculate the number, then press   and the letter name of the location. To retrieve it, press  and the letter name of the location.

**Example 1:** Store 0.12 in location A, which is above the MATH key:

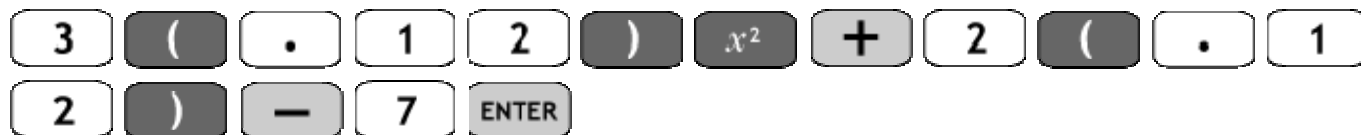


**Example 2:** Retrieve the number stored in memory location A:



**Example 3:** Evaluate  $3A^2 + 2A - 7$  when  $A = 0.12$ .

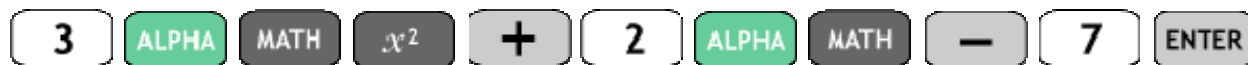
Recall: "Evaluate" means to substitute 0.12 in place of A, then do the resulting arithmetic.

Method 1: Substitute  $3(0.12)^2 + 2(0.12) - 7$ , then use the calculator:

```

3(.12)^2+2(.12)-7
-6.7168

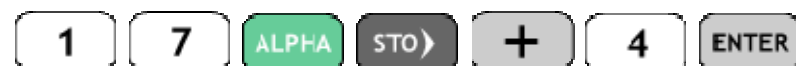
```

Answer: -6.7168Method 2: If you did not store 0.12 in A, do it now. After we type the expression  $3A^2 + 2A - 7$ , the GC will automatically substitute the value 0.12 for each A in the expression and do the arithmetic.

```

A      .12
3A^2+2A-7
-6.7168

```

Answer: -6.7168**Example 4:** Evaluate  $2x^2 - 17x + 4$  when  $x = 3.5$ Note: Use **ALPHA** **STO>** for memory location x, not the graphing variable **X,T,Θ,n**.

```

3.5→X      3.5
2X^2-17X+4  -31

```

Answer: -31



Memory locations can be used for several variables simultaneously.

**Example 5:** Evaluate  $5x^3 - 3xyz + 2x^2y - 7yz^2 - y^3 + z^3$  when  $x = 3.5$ ,  $y = -1.7$ , and  $z = 2.9$ .

If you are tempted to skip this example because it's long and ugly, don't! The next example uses this same expression, but if you do it now, you'll only have to type it once.  
Take a deep breath; here we go!

Step 1: Store all the values of the variables.

Check that x is still the same value from Example 4:

ALPHA STO ENTER

Store the value for y:

(-) 1 . 7 STO ALPHA 1 ENTER

Store the value for z:



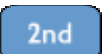



2 . 9 STO ALPHA 2 ENTER

X	3.5
-1.7→Y	-1.7
2.9→Z	2.9
■	

Step 2: Type the expression.
5 ALPHA STO ^ 3 - 3 ALPHA STO ALPHA 1 ALPHA  
2 + 2 ALPHA STO x² ALPHA 1 - 7 ALPHA 1  
ALPHA 2 x² - ALPHA 1 ^ 3 + ALPHA 2 ^  
3 ENTER

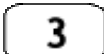
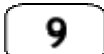

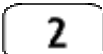

5X^3-3XYZ+2X^2Y-7
YZ^2-Y^3+Z^3
353.871

Step 3: Round the result.Answer: 353.871

That last expression was pretty nasty-looking, and most people would rather not type it again. Fortunately, the GC keeps the last fifteen calculations, which we can access using ENTRY, the 2<sup>nd</sup> function above ENTER. To get the most recent entry, type  . To see the entry before the most recent entry, press   again. On newer models of the TI-84+, you can use the directional arrows   to move to the desired entry, then press ENTER.

**Example 6:** Evaluate  $5x^3 - 3xyz + 2x^2y - 7yz^2 - y^3 + z^3$  when  $x = 3.5$ ,  $y = -1.7$ , and  $z = 3.9$ . Notice that this expression is identical to the previous question, only the value for  $z$  is changed.

Step 1: Store the new value of  $z$ . (We don't need to store  $x$  and  $y$  again; they're still there.)

Step 2: Use ENTRY to avoid re-typing. The previous entry is now what we just did, storing the new  $z$  value, so we want two entries back.

gives the first most recent entry

```

5X^3-3XYZ+2X^2Y-7
YZ^2-Y^3+Z^3
353.871
3.9+Z
3.9
3.9+Z

```

We type again:

to get the second most recent entry

```

5X^3-3XYZ+2X^2Y-7
YZ^2-Y^3+Z^3
353.871
3.9+Z
3.9
5X^3-3XYZ+2X^2Y-7
YZ^2-Y^3+Z^3

```

We press  to execute this command.

```

YZ^2-Y^3+Z^3
353.871
3.9+Z
3.9
5X^3-3XYZ+2X^2Y-7
YZ^2-Y^3+Z^3
487.571




```

Step 3: Round the result.

Answer: 487.571

Notice, the GC used the new value for  $z$ , so the answer is different from the answer in Example 5.












Not only can we use the previous entries, but we can edit them by typing over or using delete

 or using insert (INS is  ). In this way, we can avoid re-typing similar entries.

**Example 7:** (no editing yet): Evaluate  $2x^2 - 7x + 5$  when  $x = 2.1$ .

Store value in x:       

Type the expression:

2.1→X	
2X <sup>2</sup> -7X+5	2.1
	-.88







Answer: -.88

**Example 8:** (type over the previous): Evaluate  $3x^2 - 5x + 10$  when  $x = 2.1$


Step 1: Retrieve the previous entry.  

Step 2: Edit the previous entry.

Use the left arrow to move the cursor on top of the 2, and type 3 instead. Similarly, use the right arrow to move to the 7 and change it to 5, and to the 5 and change it to 10.

 (8 times)   (3 times)     


2.1→X	
2X <sup>2</sup> -7X+5	2.1
	-.88
3X <sup>2</sup> -5X+10	
	12.73

Step 3: Check the expression on your screen, and press .

Answer: 12.73

**TI-84+ GC 5 Memory Locations and Editing Using Answer, Entry, Delete, and Insert**, page 6**Example 9:** (delete from previous): Evaluate  $x^2 - 5x + 1$  when  $x = 2.1$ Step 1: Retrieve the previous entry.  Step 2: Use the left arrow to move the cursor on top of the 3 and delete it. Then move on top of the 0 and delete it. (9 times)   (7 times)  

	2.1
$2X^2 - 7X + 5$	-.88
$3X^2 - 5X + 10$	12.73
$X^2 - 5X + 1$	-5.09

Step 3: Check the expression on your screen and press Answer: -5.09**Example 10:** (using insert, which is 2<sup>nd</sup> DEL): Evaluate  $37x^2 - 58x + 146$  when  $x = 2.1$ Note: INSERT puts typed text in front of the cursor's location.Step 1: Retrieve the previous entry.  Step 2: Use the left arrow to move the cursor on top of the x of  $x^2$  and insert 37:Press  (7 times)    .Move on top of the x and insert 8.       .Move to the right of 1 and type 46 to get 146.  (3 times)   

	-.88
$3X^2 - 5X + 10$	12.73
$X^2 - 5X + 1$	-5.09
$37X^2 - 58X + 146$	187.37

Step 3: Check the expression on your screen and press Answer: 187.37

**TI-84+ GC 5 Memory Locations and Editing Using Answer, Entry, Delete, and Insert, page 7**

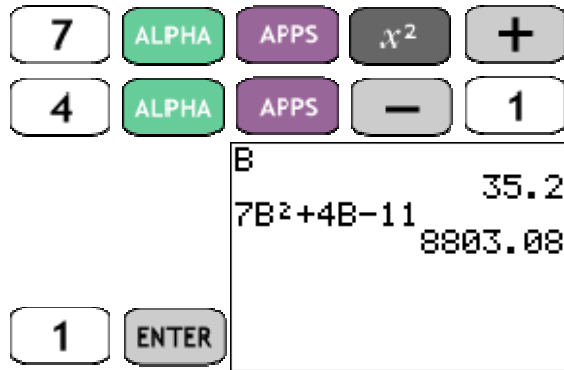
Practice:

- 1) Evaluate  $7B^2 + 4B - 11$  when  $B = 35.2$ . Answer: \_\_\_\_\_
- 2) Evaluate  $-2C^2 + 5C + 9$  when  $C = 0.109$ . Round to the nearest ten-thousandth.  
Answer: \_\_\_\_\_
- 3) Evaluate  $-2A^2 + 5A + 9$  when  $A = 0.109$ . Round to the nearest tenth.  
Answer: \_\_\_\_\_
- 4) Does changing the name of the variable (or the name of the memory location) change the result?  
Answer: \_\_\_\_\_
- 5) Evaluate  $A^2 + B^2 + C^2$  when  $A = 0.109$ ,  $B = 35.2$ , and  $C = 7.06$ . Round to the nearest tenth.  
Answer: \_\_\_\_\_
- 6) Evaluate  $2D^3 - 3E^2 + 4F$  when  $D = 17$ ,  $E = 18$  and  $F = 19$  Answer: \_\_\_\_\_
- 7) Evaluate  $5x^3 - 3xyz + 2x^2y - 7yz^2 + 4xz^2 - y^3 + z^3$  when  $x = 3.5$ ,  $y = -1.7$ , and  $z = 4.1$ .  
Answer: \_\_\_\_\_
- 8) Evaluate  $5x^3 - 3xyz + 2x^2y - 7yz^2 + 4xz^2 - y^3 + z^3$  when  $x = -3.5$ ,  $y = -1.7$ , and  $z = 4.1$ .  
Answer: \_\_\_\_\_
- 9) Evaluate  $5x^3 - 3xyz + 2x^2y - 7yz^2 + 4xz^2 - y^3 + z^3$  when  $x = -3.5$ ,  $y = 1.9$ , and  $z = 4.3$ .  
Note: both the y and z changed. This means the expression will be three entries back.  
Answer: \_\_\_\_\_
- 10) Evaluate  $4x^2 + 8x + 13$  when  $x = 2.1$ . Answer: \_\_\_\_\_
- 11) Evaluate  $372x^2 + 589x + 1460$  when  $x = 2.1$  Answer: \_\_\_\_\_
- 12) Evaluate  $7x^2 + 9x - 1$  when  $x = 2.1$  Answer: \_\_\_\_\_
- 13) Evaluate  $72x^2 + 9x - 13$  when  $x = 7.3$  Answer: \_\_\_\_\_  
Note: the x-value changed, too.
- 14) Evaluate  $-35x^2 + x - 2$  when  $x = -8.1$  Answer: \_\_\_\_\_
- 15) Evaluate  $-3x^2 + 9x - 23$  when  $x = -5.3$  Answer: \_\_\_\_\_

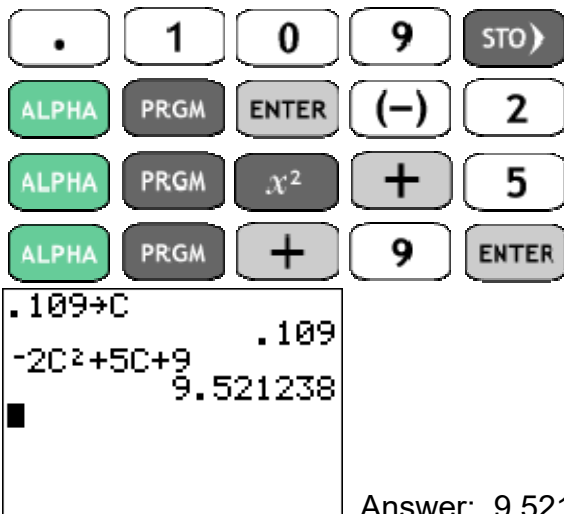
# TI-84+ GC 5 Memory Locations and Editing Using Answer, Entry, Delete, and Insert, solutions

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1)

Answer: 8803.08

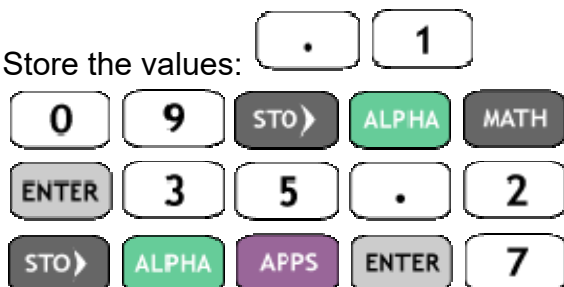
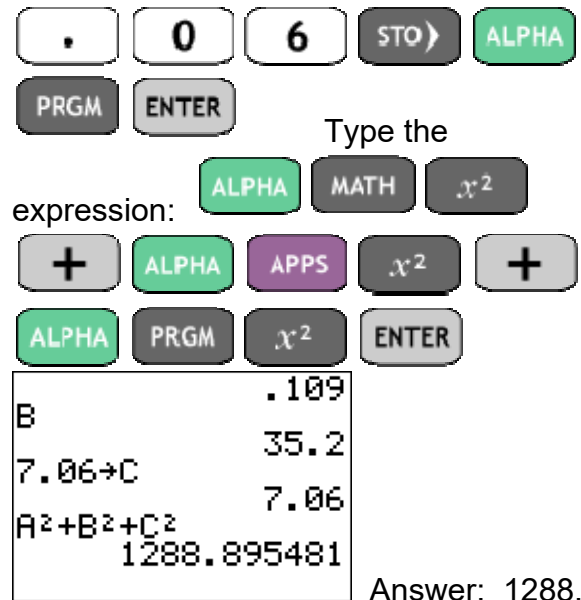
2)

Answer: 9.5212

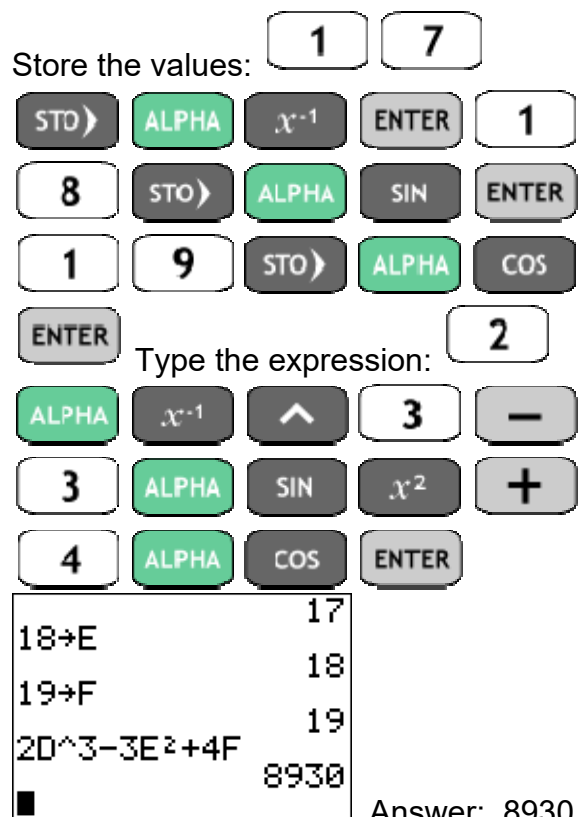
3) same calculation as the previous question, only rounded differently.  
Answer: 9.5

4) No. Changing the name does not change the result when evaluating variables at given values.

5) Store the values:

Answer: 8930Answer: 1288.9

6) Store the values:

Answer: 8930

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7) Store the values:

Calculator keypad sequence for problem 7:

Row 1:  $3$ ,  $.$ ,  $5$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $\text{STO} \rightarrow$ ,  $\text{ENTER}$ ,  $(-)$ ,  $1$

Row 2:  $.$ ,  $7$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $1$ ,  $\text{ENTER}$ ,  $4$ ,  $.$ ,  $1$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$

Row 3:  $2$ ,  $\text{ENTER}$

Text: Type the expression:

Row 4:  $5$ ,  $\text{ALPHA}$ ,  $\text{STO} \rightarrow$ ,  $\wedge$ ,  $3$ ,  $-$ ,  $3$

Row 5:  $\text{ALPHA}$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $1$ ,  $\text{ALPHA}$ ,  $2$ ,  $+$ ,  $2$ ,  $\text{ALPHA}$ ,  $\text{STO} \rightarrow$ ,  $x^2$

Row 6:  $\text{ALPHA}$ ,  $1$ ,  $-$ ,  $7$ ,  $\text{ALPHA}$ ,  $1$ ,  $\text{ALPHA}$ ,  $2$ ,  $x^2$ ,  $+$ ,  $4$

Row 7:  $\text{ALPHA}$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $2$ ,  $x^2$ ,  $-$ ,  $\text{ALPHA}$ ,  $1$ ,  $\wedge$ ,  $3$ ,  $+$

Calculator screen display:

```

-1.7
4.1 ÷ Z
4.1
5X^3-3XYZ+2X^2Y-7
YZ^2+4XZ^2-Y^3+Z^3
755.123
  
```

Row 8:  $\text{ALPHA}$ ,  $2$ ,  $\wedge$ ,  $3$ ,  $\text{ENTER}$

Answer: 755.123

8) Store the new x value:

Calculator keypad sequence for problem 8:

Row 1:  $(-)$ ,  $3$ ,  $.$ ,  $5$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $\text{STO} \rightarrow$ ,  $\text{ENTER}$

Text: Back

Calculator screen display:

```

755.123
-3.5 ÷ X
-3.5
5X^3-3XYZ+2X^2Y-7
YZ^2+4XZ^2-Y^3+Z^3
-290.677
  
```

Row 2:  $2^{\text{nd}}$ ,  $\text{ENTER}$ ,  $2^{\text{nd}}$ ,  $\text{ENTER}$ ,  $\text{ENTER}$

two entries:

Answer: -290.677

9) Store new values for y and z:

Calculator keypad sequence for problem 9:

Row 1:  $1$ ,  $.$ ,  $9$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $1$ ,  $\text{ENTER}$ ,  $4$

Row 2:  $.$ ,  $3$ ,  $\text{STO} \rightarrow$ ,  $\text{ALPHA}$ ,  $2$ ,  $\text{ENTER}$

Text: Back three entries:

Calculator screen display:

```

1.9
4.3 ÷ Z
4.3
5X^3-3XYZ+2X^2Y-7
YZ^2+4XZ^2-Y^3+Z^3
-514.169
  
```

Row 3:  $\text{ENTER}$ ,  $2^{\text{nd}}$ ,  $\text{ENTER}$ ,  $\text{ENTER}$

Answer: -514.169

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10)

2.1 ÷ X	2.1
4X²+8X+13	47.44

Answer: 47.44

11)

2.1 ÷ X	2.1
4X²+8X+13	47.44
372X²+589X+1460	4337.42

Answer: 4337.42

12)

	22.21
37X²+58X+146	430.97
372X²+589X+1460	4337.42
7X²+9X-1	48.77

Answer: 48.77

13) New value of x:

372X²+589X+1460	4337.42
7X²+9X-1	48.77
7.3 ÷ X	7.3
	7.3

Back two entries:

7X²+9X-1	48.77
7.3 ÷ X	7.3
	7.3
72X²+9X-13	3889.58

Answer: 3889.58



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14) New value of x:  $(-)$  8 . 1  $\text{STO} \rightarrow$  ALPHA  $\text{STO} \rightarrow$  ENTER . Back two  
 entries: 2nd ENTER 2nd ENTER < (10 times) 2nd DEL (insert)  $(-)$   
 3 5 (delete extras) DEL DEL > (3 times) DEL > >  
 2 DEL ENTER

$$\begin{array}{r} -8.1 \div X \\ -35X^2 + X - 2 \\ \hline -2306.45 \end{array}$$

Answer: -2306.45

15) New value of x:  $(-)$  5 . 3  $\text{STO} \rightarrow$  ALPHA  $\text{STO} \rightarrow$  ENTER Back two  
 entries: 2nd ENTER 2nd ENTER < (6 times) DEL > (3 times) 2nd  
 DEL 9 > (3 times) 3 ENTER

$$\begin{array}{r} -8.1 \\ -35X^2 + X - 2 \\ \hline -2306.45 \\ -5.3 \div X \\ -3X^2 + 9X - 23 \\ \hline -154.97 \end{array}$$

Answer: -154.97